Phenomenological extraction of Transverse Momentum Dependent distributions

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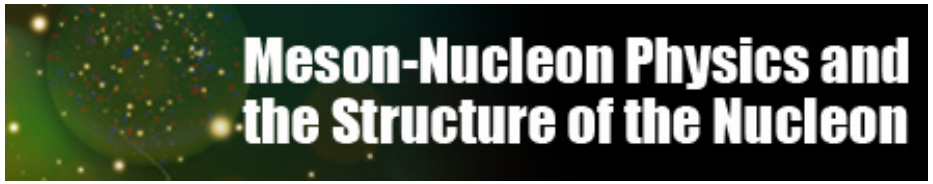
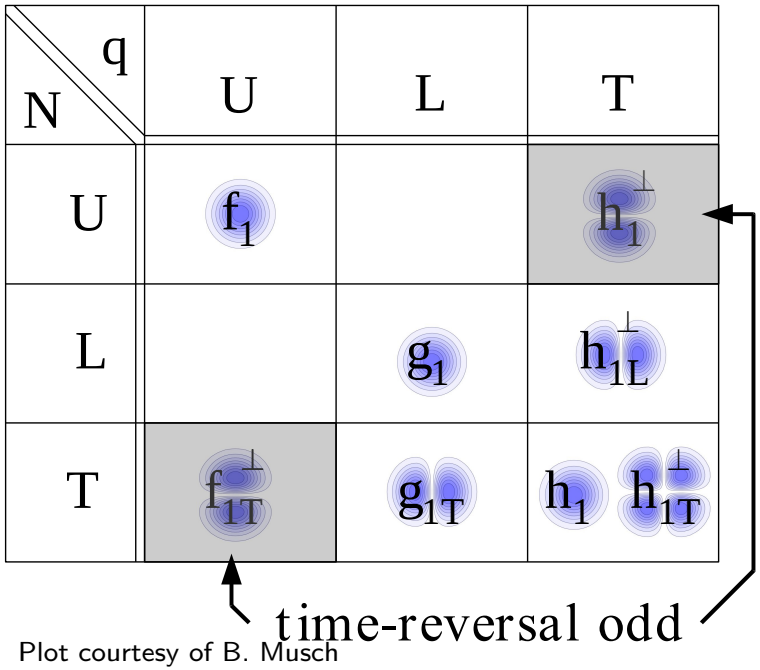


Transverse Momentum Dependent distributions

Spin structure of spin-1/2 nucleon is described by 8 TMDs. Each of them depend on two indipendent variables x and $\mathbf{k}_\perp$.



Plot courtesy of B. Musch

Kotzinian 1995;

Mulders, Tangerman 1995; Boer and Mulders 1997; Bacchetta et al 2007

T-odd TMDs – Sivers and Boer-Mulders functions survive due to Final State Interactions.

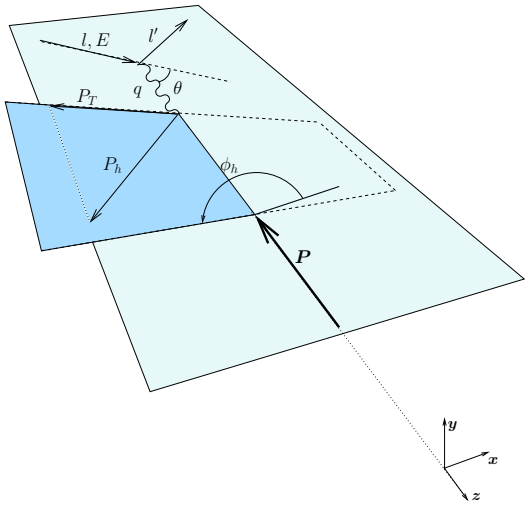
Polarised Semi Inclusive Deep Inelastic Scattering

Asymmetry in $\gamma^* p$ cm frame of $\ell p^\uparrow \to \ell' h X$

TMD functions can be studied in asymmetries

$$A_{UT} = \frac{d\sigma^\uparrow - d\sigma^\downarrow}{\frac{1}{2}(d\sigma^\uparrow + d\sigma^\downarrow)}$$

Unpolarised electron beam, Transversely polarised proton. Azimuthal dependence on Φ_h and Φ_S singles out different combinations.



Contributions at leading twist

$$d\sigma^\uparrow - d\sigma^\downarrow \propto \underbrace{f_{1T}^\perp \otimes d\hat{\sigma} \otimes D_{h/q} \sin(\phi_h - \phi_S)}_{\text{Sivers effect}} +$$

$$+ \underbrace{h_1 \otimes \Delta\hat{\sigma}^\uparrow \otimes H_1^\perp \sin(\phi_h + \phi_S)}_{\text{Collins effect}} +$$

$$+ \ldots$$

Kotzinian 1995;

Mulders, Tangerman 1995; Boer and Mulders 1997; Bacchetta et al 2007

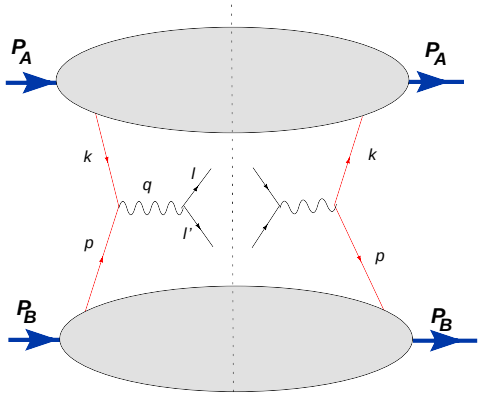
Sivers function: process dependence

Sivers function Sivers 1990 can be measured in both SIDIS and DY processes.

$$f_{q/P^\uparrow}(x, \mathbf{k}_\perp, S) = f_1(x, \mathbf{k}_\perp^2) - \frac{S \cdot (\hat{P} \times k_\perp)}{M} f_{1T}^\perp(x, \mathbf{k}_\perp^2)$$

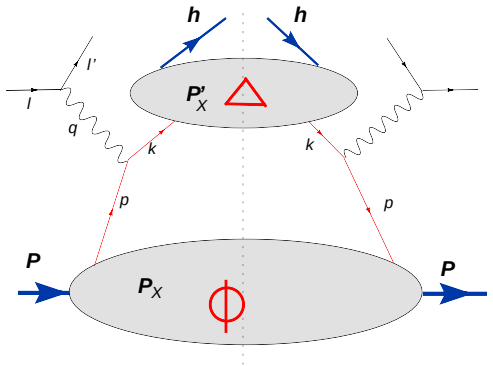
Drell Yan $A^\uparrow B \longrightarrow l^+ l^- X$

$$A_{UT}^{sin(\phi_\gamma - \phi_S)} \sim f_{1T}^{\perp DY}(x, k_\perp) \otimes f_{\bar{q}/B}(x, p_\perp)$$



SIDIS $\ell P^\uparrow \longrightarrow \ell' h X$

$$A_{UT}^{sin(\phi_H - \phi_S)} \sim f_{1T}^{\perp SIDIS}(x, k_\perp) \otimes D_{h/q}(z, p_\perp)$$

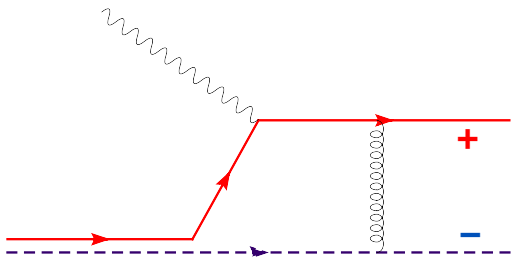


Modified universality

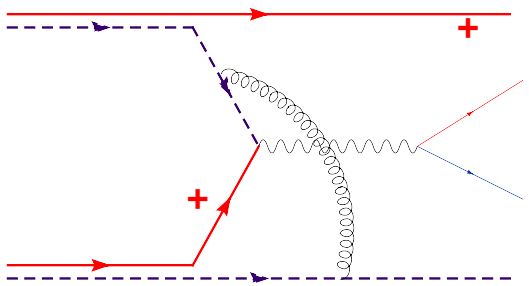
Sivers function is process dependent. Collins 2002

$$f_{1T}^{\perp DY} = -f_{1T}^{\perp SIDIS}$$

Let's consider a simple model of Final State Interactions as in Brodsky, Hwang, Schmidt 2002,
proton = quark$^+$ + antiquark$^-$



SIDIS - attractive

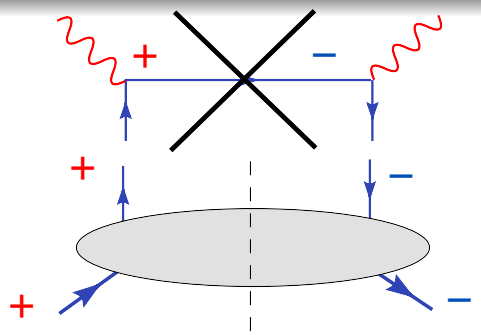


DY - repulsive

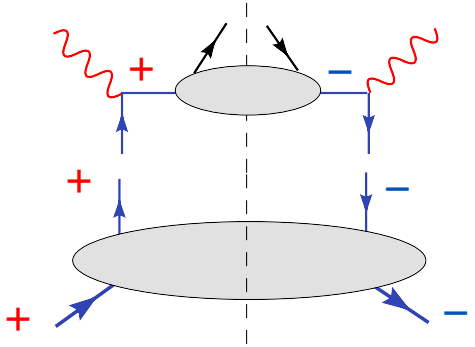
• Experimental test of this relation is fundamental for our understanding of the origin of the correlation between parton angular momentum and the spin of the proton and the gauge link formalism itself.
Experimental DY data are not available, experiments are planned.

TRANSVERSITY

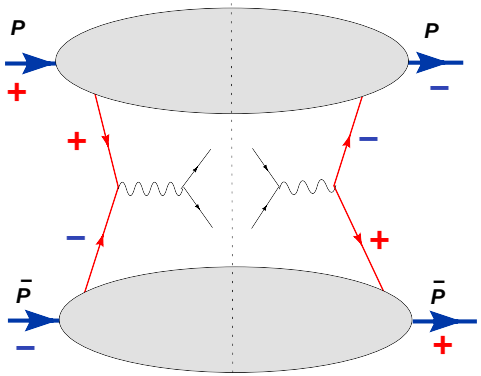
Transversity cannot be studied in DIS as QED and QCD interactions conserve helicity up to corrections $\mathcal{O}(m_q/E)$.



Transversity can be measured if coupled with another chiral-odd function. This can be done in Semi Inclusive DIS (SIDIS), quark fragments into unpolarised hadron. It couples to so called Collins Fragmentation function that describes how a polarised quark fragments into unpolarised hadron.

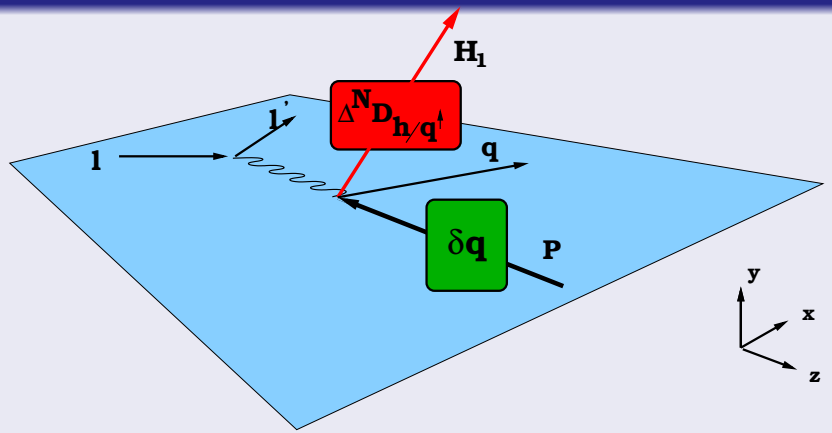


Golden channel to study transversity is proton - antiproton double spin asymmetry at GSI $A_N \propto h_{q/P}(x) h_{\bar{q}/\bar{P}}(x)$.

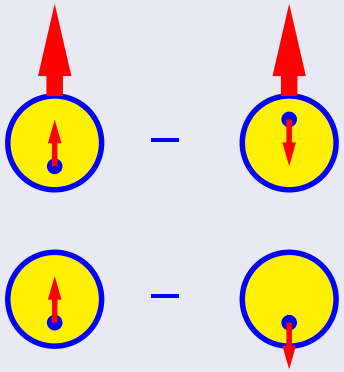


How to measure transversity? SIDIS and e^+e^- annihilation

SIDIS $lN \to l' H_1 X$



Collins effect gives rise to azimuthal Single Spin Asymmetry

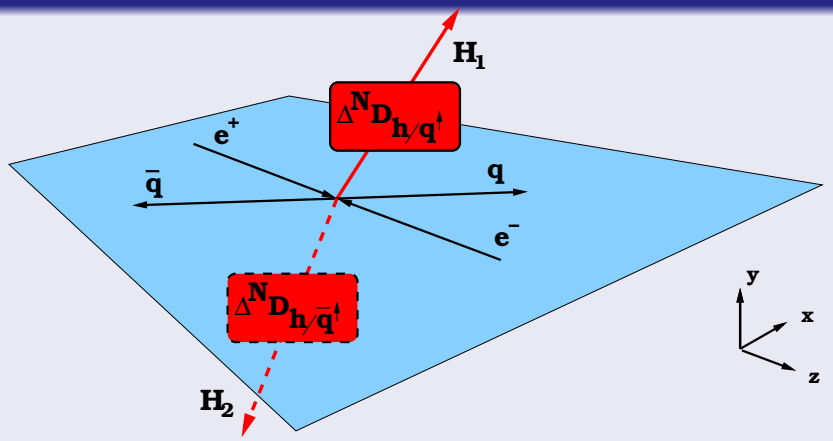


$= \Delta_T q(x, Q^2)$

$= \Delta^N D_{h/q^\uparrow}(z, Q^2)$

J. C. Collins, *Nucl. Phys.* **B396** (1993) 161

$e^+e^- \to H_1 H_2 X$



Collins effect gives rise to azimuthal asymmetry, q and $\bar{q}$ Collins functions are present in the process:

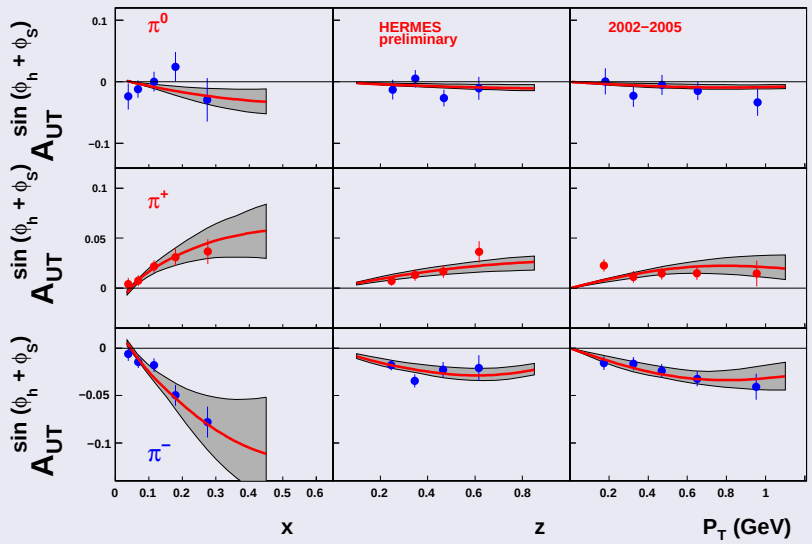
$\Delta^N D_{h/q^\uparrow}(z_1, Q^2)$

$\Delta^N D_{h/\bar{q}^\uparrow}(z_2, Q^2)$

D. Boer, R.Jacob and P. J. Mulders *Nucl. Phys.* **B504** (1997) 345

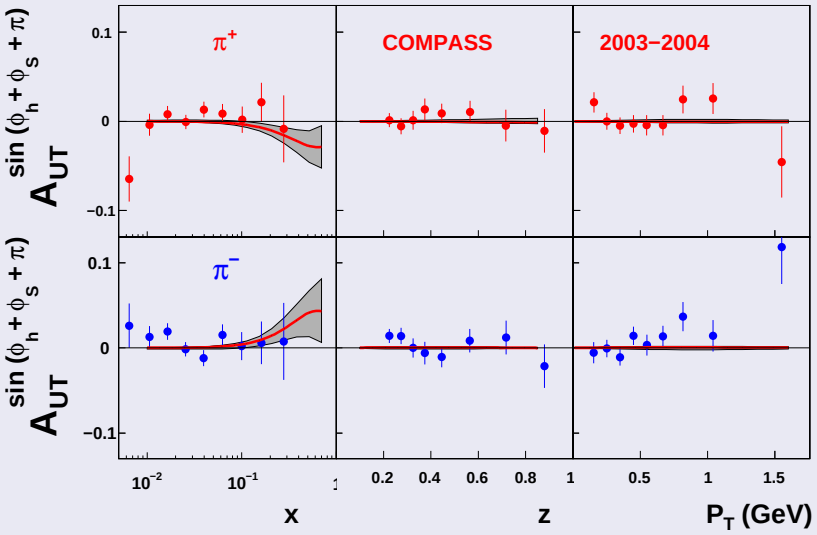
Experimental data

HERMES $A_{UT}^{sin(\phi_h+\phi_S)}$



$ep \to e\pi X$, $p_{lab} = 27.57$ GeV.

COMPASS $A_{UT}^{sin(\phi_h+\phi_S+\pi)}$



$\mu D \to \mu\pi X$, $p_{lab} = 160$ GeV

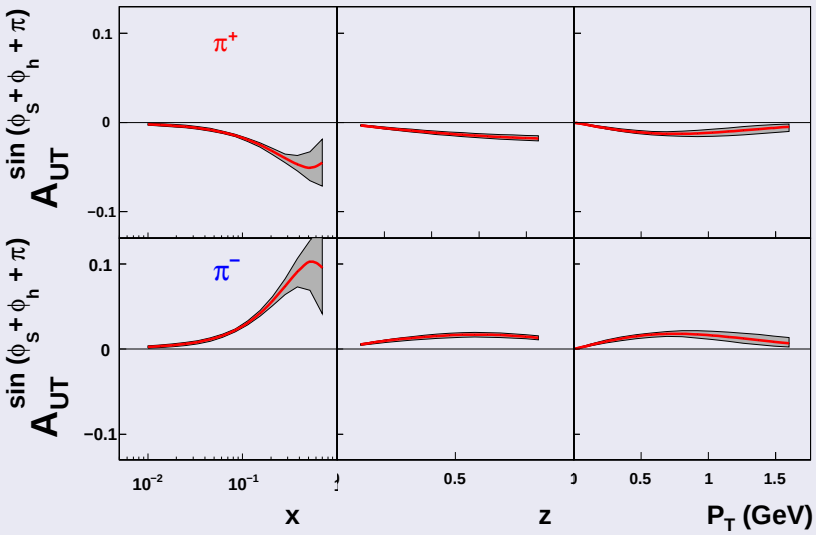
HERMES, M. Diefenthaler, (2007),arXiv:0706.2242

COMPASS, M. Alekseev et al., (2008), Phys.Lett.B673:127-135,2009

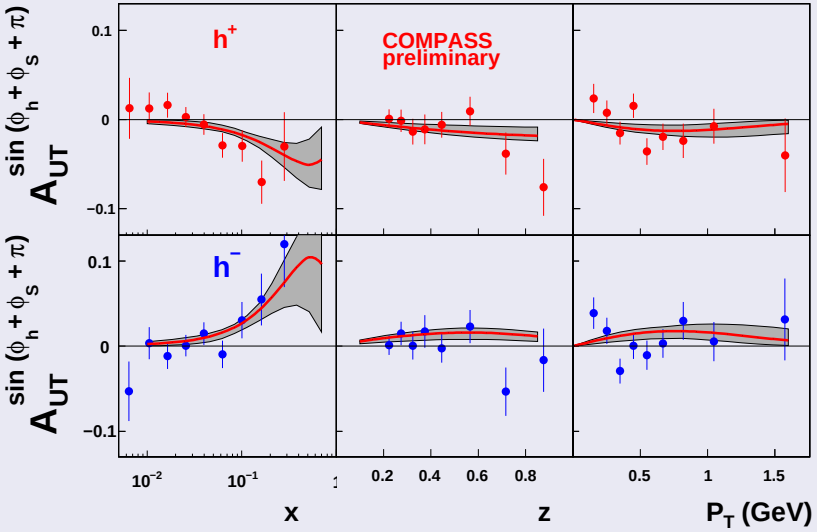
Description of the data

Predictions for COMPASS operating on PROTON target

COMPASS $A_{UT}^{sin(\phi_h+\phi_S+\pi)}$



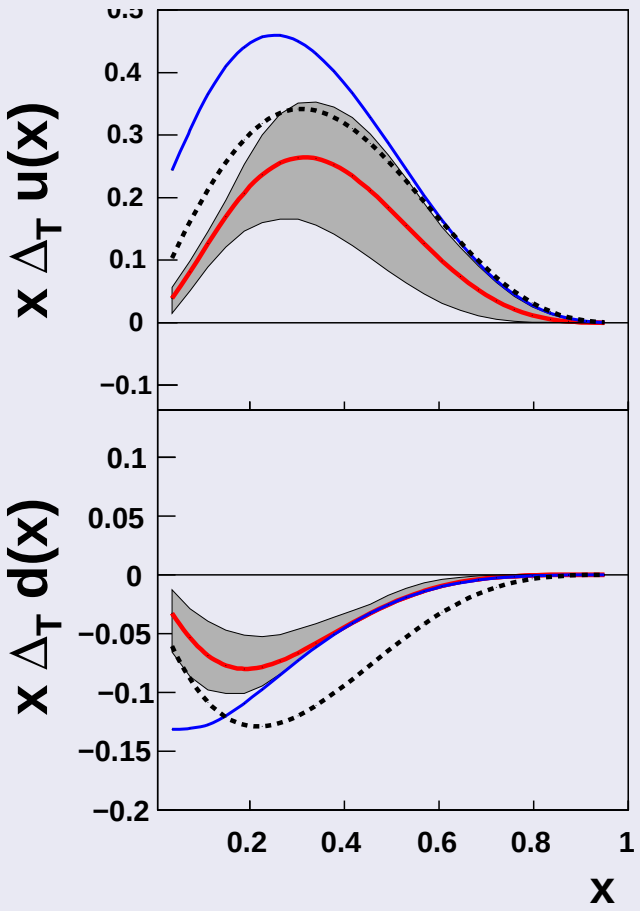
COMPASS $A_{UT}^{sin(\phi_h+\phi_S+\pi)}$



Comparison with preliminary COMPASS data arXiv:0808.0086

Anselmino et al 2009

Transversity vs. helicity



1. Solid red line – transversity distribution

$$\Delta_T q(x)$$

this analysis at $Q^2 = 2.4$ GeV^2.

2. Solid blue line – Soffer bound

$$|\Delta_T q(x)| < \frac{q(x) + \Delta q(x)}{2}$$

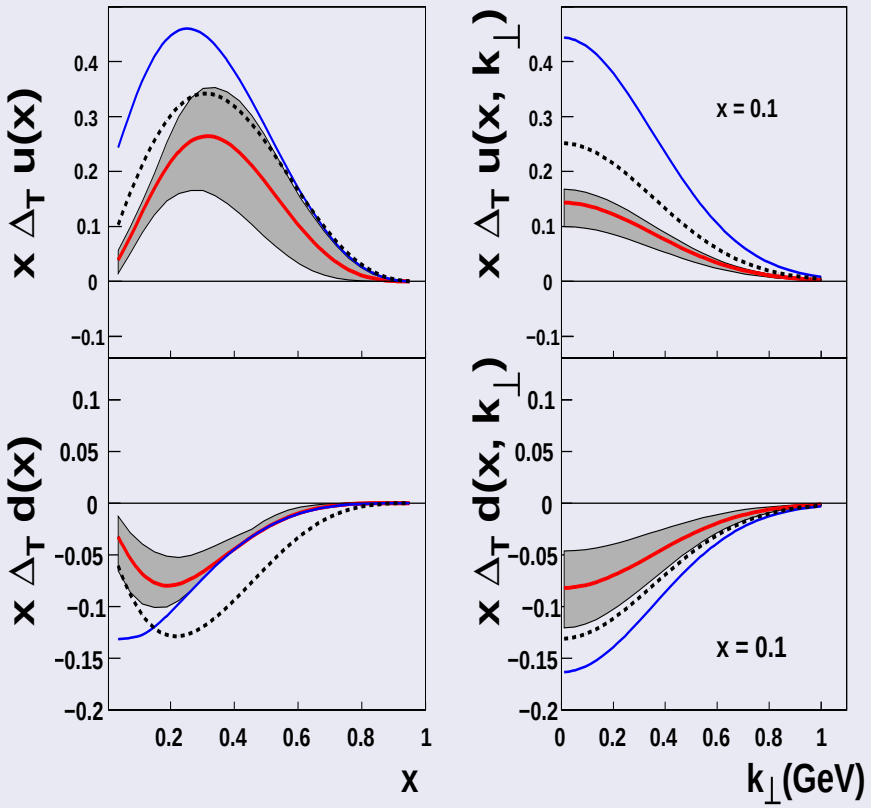
GRV98LO + GRSV98LO

3. Dashed line – helicity distribution

$$\Delta q(x)$$

GRSV98LO

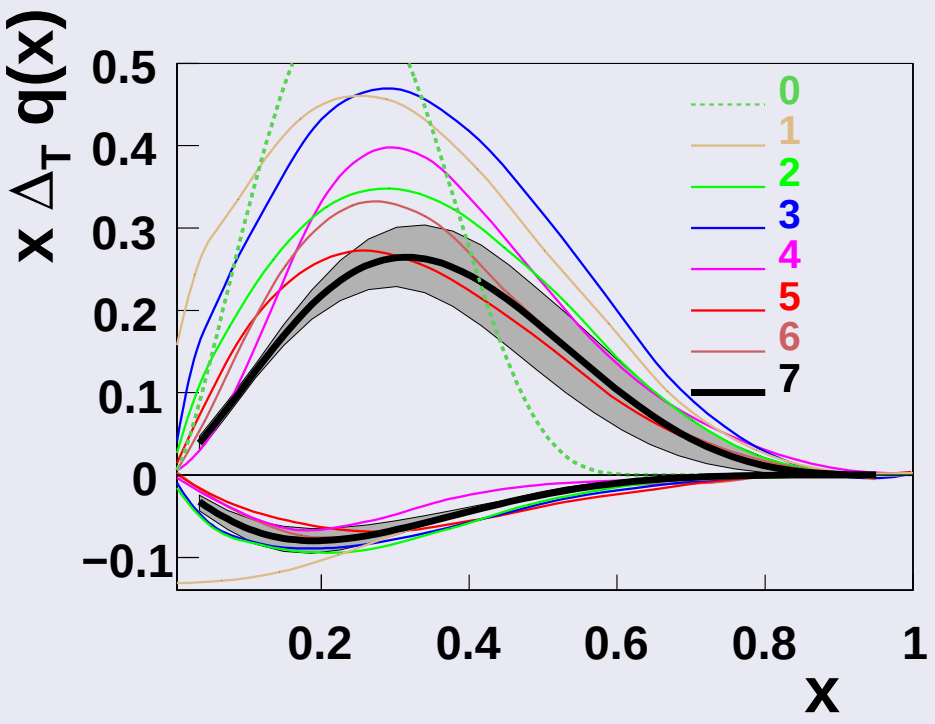
Transversity



- This is the extraction of transversity from existing experimental data. Anselmino et al 2009
- $\Delta_T u(x) > 0$ and $\Delta_T d(x) < 0$
- $|\Delta_T q(x)| < |\Delta q(x)|$.
- JLab @ 12 GeV will provide wider region of x for tensor charge extraction.

Transversity, comparison with models

New extraction is close to most models.

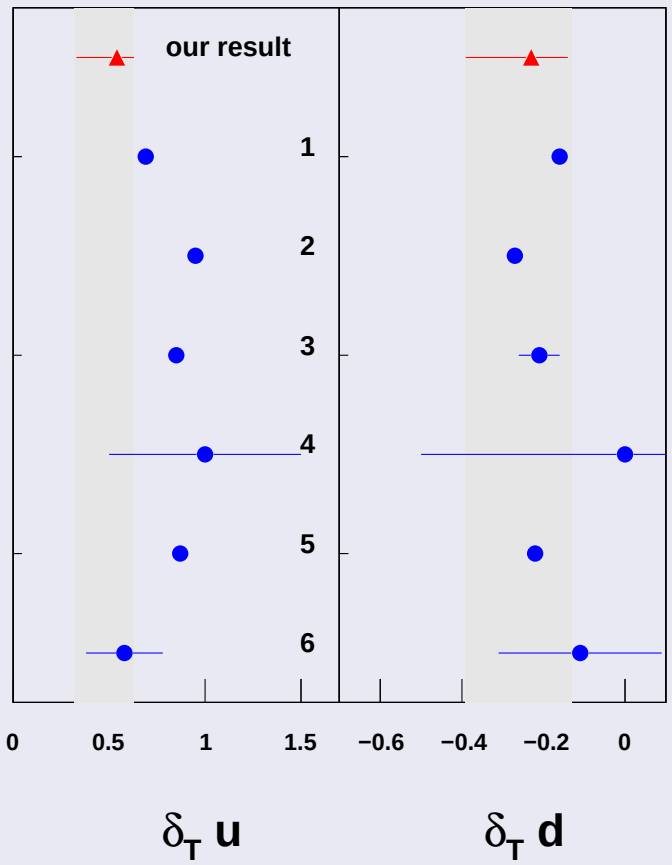


0. Barone, Calarco, Drago PLB 390 287 (97)
1. Soffer et al. PRD 65 (02)
2. Korotkov et al. EPJC 18 (01)
3. Schweitzer et al. PRD 64 (01)
4. Wakamatsu, PLB B653 (07)
5. Pasquini et al., PRD 72 (05)
6. Cloet, Bentz and Thomas PLB 659 (08)
7. Anselmino et al 2009.

Tensor charges

$$\delta_T q = \int_0^1 dx\,(h_{1q} - h_{1\bar{q}}) = \int_0^1 dx\, h_{1q}$$

$\delta_T u = 0.54^{+0.09}_{-0.22}$, $\delta_T d = -0.23^{+0.09}_{-0.16}$ at $Q^2 = 0.8$ GeV^2



1. Quark-diquark model:
   Cloet, Bentz and Thomas
   PLB **659**, 214 (2008), $Q^2 = 0.4$ GeV^2
2. CQSM:
   M. Wakamatsu, PLB **653** (2007) 398.
   $Q^2 = 0.3$ GeV^2
3. Lattice QCD:
   M. Gockeler et al.,
   Phys.Lett.B627:113-123,2005 ,
   $Q^2 = 4$ GeV^2
4. QCD sum rules:
   Han-xin He, Xiang-Dong Ji,
   PRD 52:2960-2963,1995, $Q^2 \sim 1$ GeV^2
5. Constituent quark model:
   B. Pasquini, M. Pincetti, and S. Boffi,
   PRD72(2005)094029 and PRD76(2007)034020,
   $Q^2 \sim 0.8$ GeV^2
6. Spin-flavour SU(6) symmetry
   L. Gamberg, G. Goldstein,
   Phys.Rev.Lett.87:242001,2001 $Q^2 \sim 1$ GeV^2

Sivers effect

The azimuthal asymmetry $A_{UT}^{sin(\phi_h - \phi_S)}$ arises due to Sivers function (Sivers 90)
Torino notations are used

$$f_{q/p^\uparrow}(x, \boldsymbol{k}_\perp) \quad = \quad f_{q/p}(x, k_\perp) + \frac{1}{2}\,\Delta^N f_{q/p^\uparrow}(x, k_\perp)\,\boldsymbol{S}_T \cdot (\hat{\boldsymbol{P}} \times \hat{\boldsymbol{k}}_\perp)$$

Spin sum rule:

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + < L_z^{q,\bar{q}} > + < L_z^G >$$

EMC result on $\Delta\Sigma = \sum_{q,\bar{q}} \Delta q \simeq 0.3$ triggered so called "Spin crisis" – only 30% of the spin of the proton is carried by quarks.
Leader, Anselmino ''A Crisis In The Parton Model: Where, Oh Where Is The Proton's Spin?'' Z.Phys.C41:239,1988

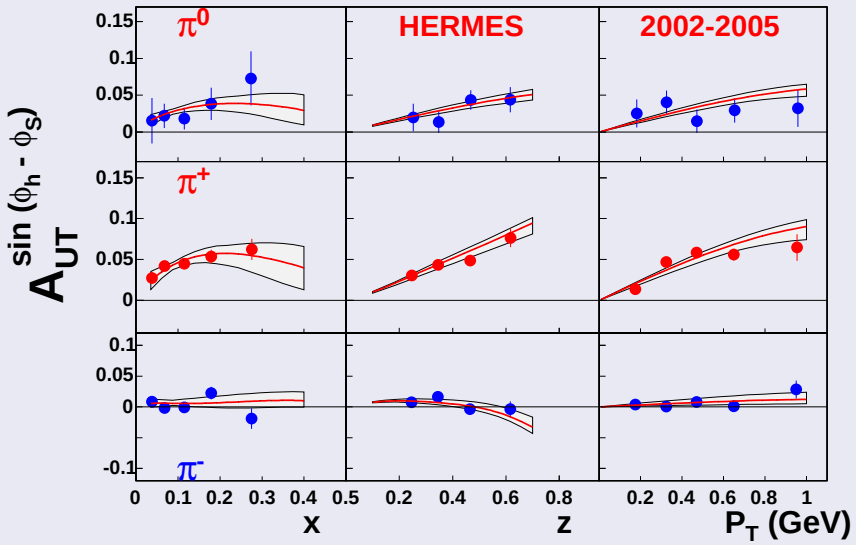
$\boldsymbol{S}_T \cdot (\hat{\boldsymbol{P}} \times \hat{\boldsymbol{k}}_\perp)$ – correlation between the spin ($\boldsymbol{S}_T$) and angular momentum ($\mathbf{L}_q$) implies non zero contribution $< L_z^{q,\bar{q}} > \neq 0$

Data are available from HERMES and COMPASS. u and d Sivers functions are non zero thus $\mathbf{L}_{u,d} \neq 0$.

HERMES and COMPASS DATA.

HERMES

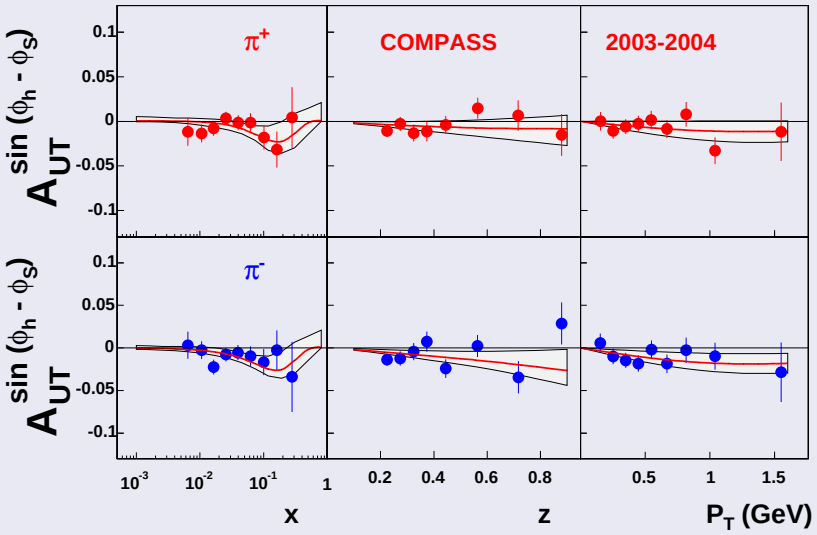
$ep \to e\pi X$, $p_{lab} = 27.57$ GeV.



M. Anselmino et al 2009

COMPASS

$\mu D \to \mu\pi X$, $p_{lab} = 160$ GeV.



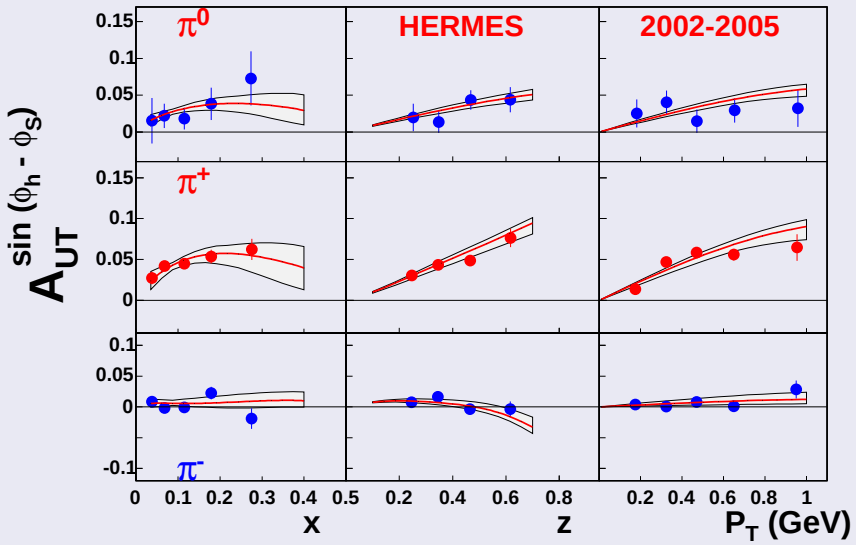
M. Anselmino et al 2009

$$lp^{\uparrow} \to l\pi^{+}X \simeq \Delta^{N}u \otimes D_{u/\pi^{+}} > 0$$
$$lp^{\uparrow} \to l\pi^{-}X \simeq 4\Delta^{N}u \otimes D_{u/\pi^{-}} + \Delta^{N}d \otimes D_{d/\pi^{-}} \simeq 0$$
$$lD^{\uparrow} \to l\pi^{+}X \simeq (\Delta^{N}u + \Delta^{N}d) \otimes D_{u/\pi^{+}} \simeq 0$$

HERMES and COMPASS DATA.

HERMES

$ep \to e\pi X$, $p_{lab} = 27.57$ GeV.



M. Anselmino et al 2009

HERMES

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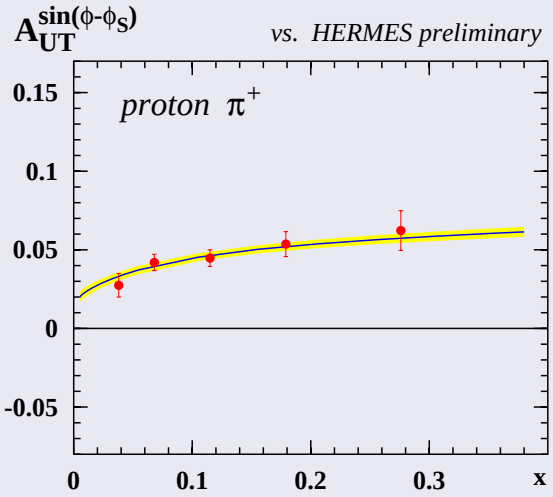
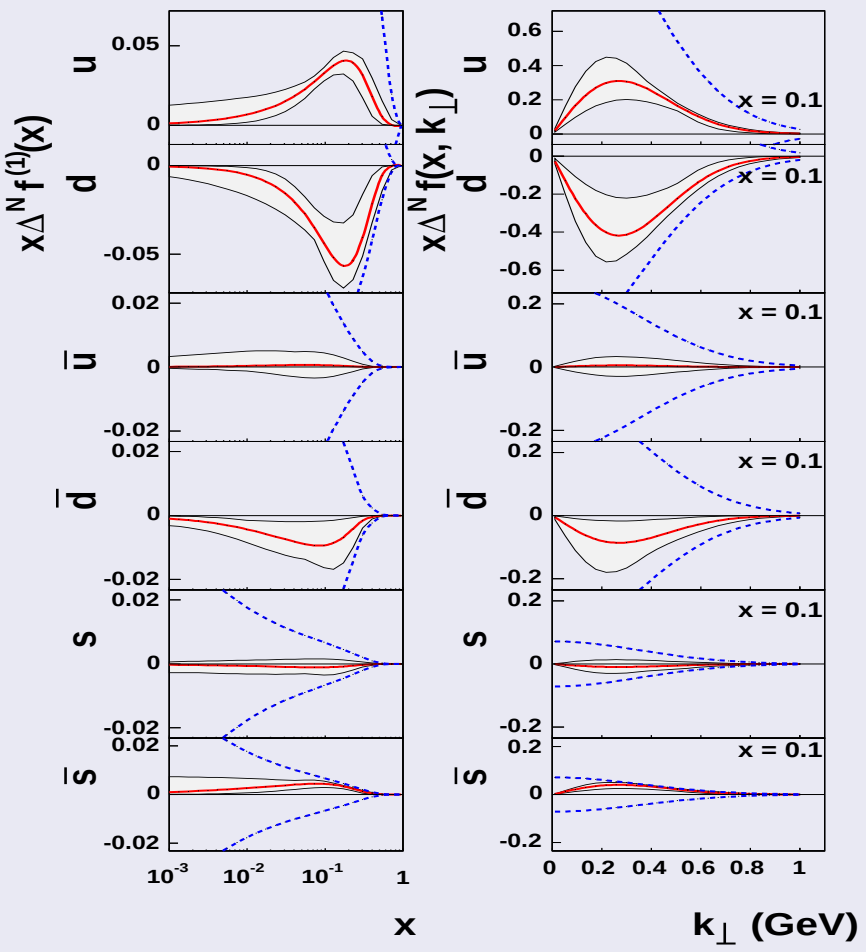


Arnold et al 2008

$$lp^{\uparrow} \to l\pi^{+}X \simeq \Delta^{N}u \otimes D_{u/\pi^{+}} > 0$$
$$lp^{\uparrow} \to l\pi^{-}X \simeq 4\Delta^{N}u \otimes D_{u/\pi^{-}} + \Delta^{N}d \otimes D_{d/\pi^{-}} \simeq 0$$
$$lD^{\uparrow} \to l\pi^{+}X \simeq (\Delta^{N}u + \Delta^{N}d) \otimes D_{u/\pi^{+}} \simeq 0$$

Sivers functions

$$\Delta^N f_q^{(1)}(x) \equiv \int d^2\boldsymbol{k}_\perp \frac{k_\perp}{4m_p} \Delta^N f_{q/p^\uparrow}(x, k_\perp) = -f_{1T}^{\perp(1)q}(x)\,.$$

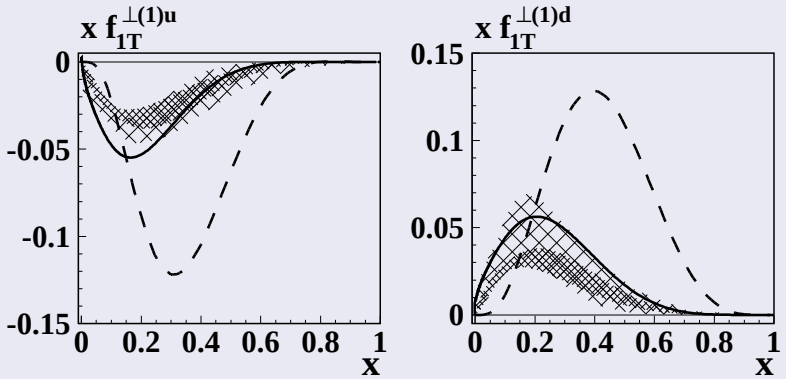


Sivers functions for u, d and sea quarks are extracted from HERMES and COMPASS data. $\Delta^N f_u > 0$, $\Delta^N f_d < 0$, first hints on nonzero sea quark Sivers functions.

Sivers function comparison with models

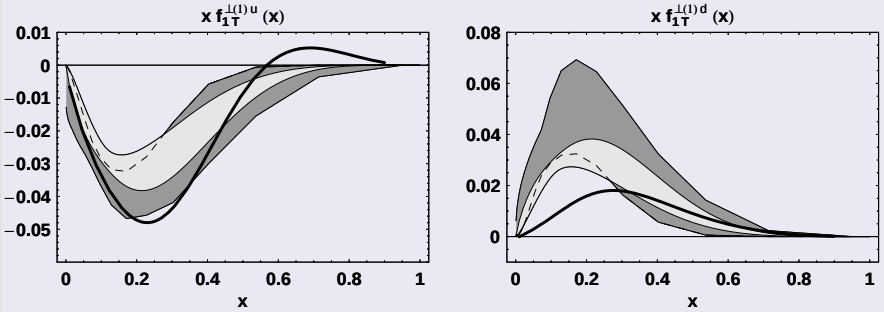
There is a number of model calculations of Sivers function
Light-cone quark model Barbara Pasquini and Feng Yuan 2010
Diquark model Alessandro Bacchetta et al 2010, Leonard Gamberg, Gary Goldstein, and Marc Schlegel 2008 etc
MIT bag model Feng Yuan 2003, H. Avakian, A.V. Efremov, P. Schweitzer, F. Yuan 2010 etc

Pasquini and Yuan 2010



Pasquini and Yuan arXiv:1001.5398

Alessandro Bacchetta et al 2010



Bacchetta et al arXiv:1003.1328

Reasonable agreement of the extracted Sivers functions Anselmino et al 2009 and Collins et al 2005 and model calculations.

Boer-Mulders effect

Boer-Mulders function

$$f_{q^\uparrow/p}(x, \boldsymbol{k}_\perp) = \frac{1}{2}\left[f_{q/p}(x, k_\perp) - h_1^{\perp q}(x, k_\perp)\,\frac{\mathbf{s}\cdot(\hat{\boldsymbol{P}}\times\boldsymbol{k}_\perp)}{M}\right]$$

Sivers function

$$f_{q/p^\uparrow}(x, \boldsymbol{k}_\perp) = f_{q/p}(x, k_\perp) - f_{1T}^{\perp q}(x, k_\perp)\,\frac{\boldsymbol{S}_T\cdot(\hat{\boldsymbol{P}}\times\boldsymbol{k}_\perp)}{M}$$

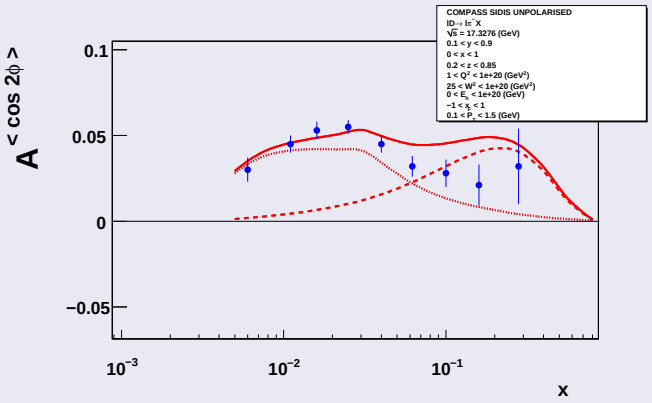
Both functions measure correlation of $(\hat{\boldsymbol{P}}\times\boldsymbol{k}_\perp)$ and $\boldsymbol{S}_T$ or $\mathbf{s}$.
Burkhadt (Burkhardt 2005) conjecture: $h_1^{\perp q}(x, k_\perp) \sim f_{1T}^{\perp q}(x, k_\perp)$, $h_1^{\perp u,d}(x, k_\perp) < 0$.

Expected values: $h_1^{\perp u}/f_{1T}^{\perp u} \simeq 1.8$, $h_1^{\perp d}/f_{1T}^{\perp d} \simeq -1$

Data are available from HERMES and COMPASS. The best fit is (Barone, AP, Melis 2010): $h_1^{\perp u}/f_{1T}^{\perp u} = 2.1 \pm 0.1$, $h_1^{\perp d}/f_{1T}^{\perp d} = -1.1 \pm 0.001$ A good accordance with expectations.

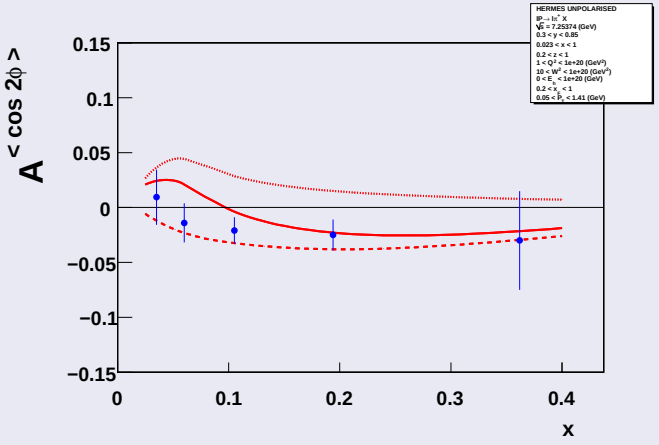
Boer-Mulders data

COMPASS $A_{UU}^{cos2\phi_h}$



Barone, Melis, AP arXiv:0912.5194

HERMES $A_{UU}^{cos2\phi_h}$



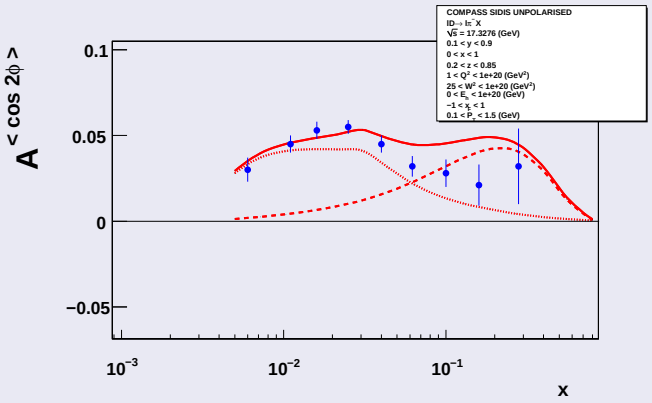
Barone, Melis, AP arXiv:0912.5194

$$F_{UU}^{\cos 2\phi_S} = h_1^\perp \otimes H_1^\perp + \frac{1}{Q^2} f_1 \otimes D_1$$

Twist-2 contribution (the dashed line) is comparable to higher twist (the dotted line) contribution at low Q^2. EIC at high Q^2 allows to measure $h_1^\perp \otimes H_1^\perp$ without higher twists.

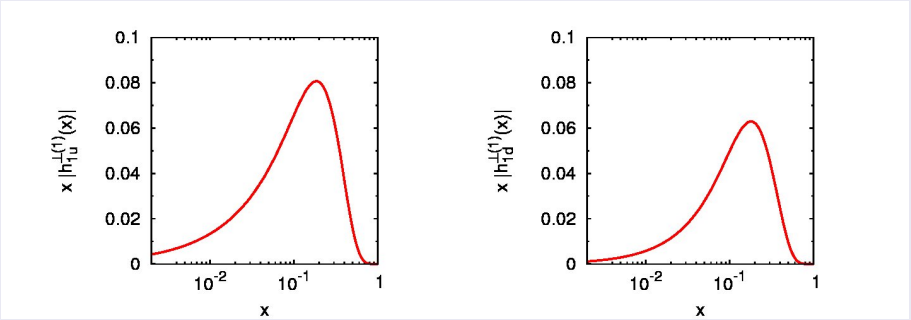
Boer-Mulders data

COMPASS $A_{UU}^{cos2\phi_h}$



Barone, Melis, AP arXiv:0912.5194

Boer-Mulders functions



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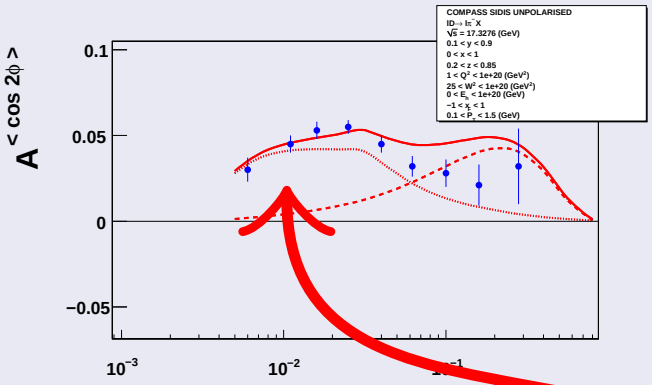
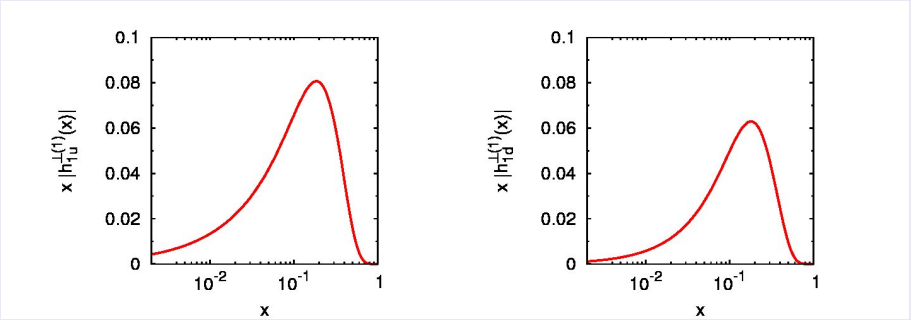
Boer-Mulders data

COMPASS $A_{UU}^{cos2\phi_h}$



Barone, Melis, AP arXiv:0912.5194

Boer-Mulders functions



$$F_{UU}^{\cos 2\phi_S} = h_1^\perp \otimes H_1^\perp + \frac{1}{Q^2} f_1 \otimes D_1$$

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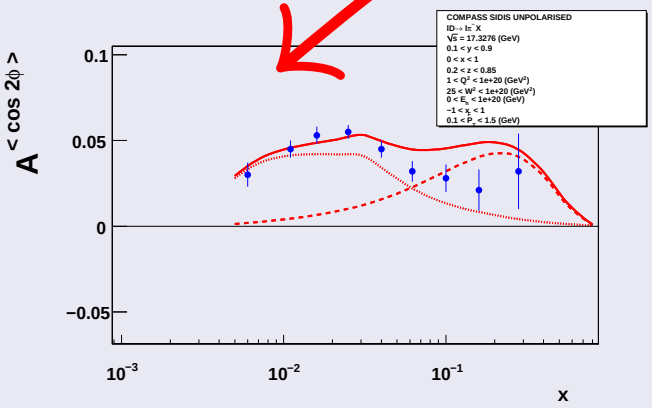

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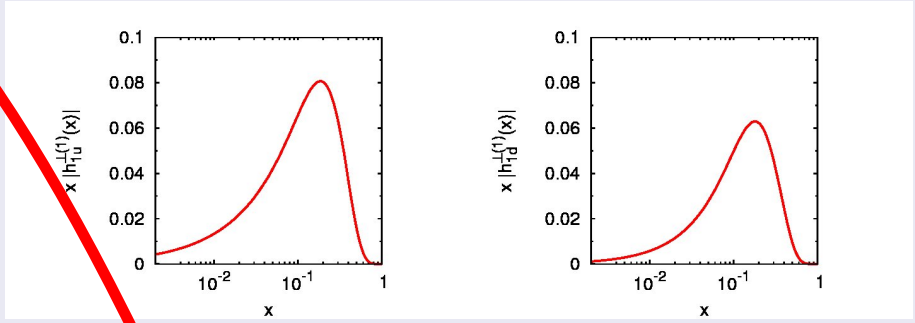

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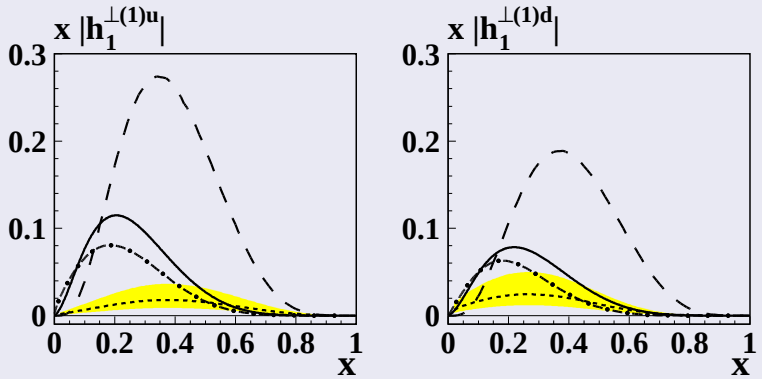
Boer-Mulders function comparison with models

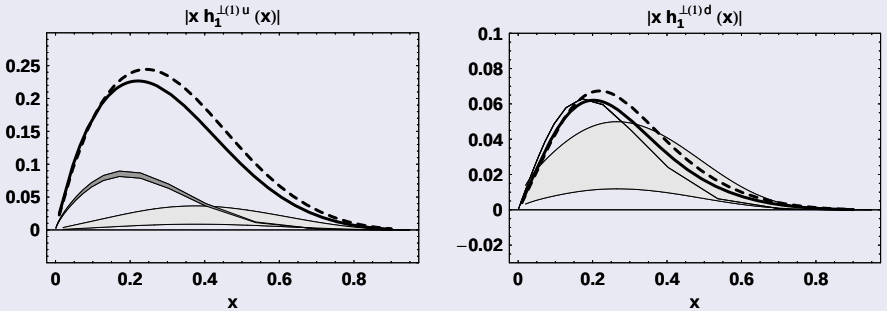
There is a number of model calculations of Boer-Mulders function
Light-cone quark model Barbara Pasquini and Feng Yuan 2010
Diquark model Alessandro Bacchetta et al 2010, Leonard Gamberg, Gary Goldstein, and Marc Schlegel 2008 etc

Pasquini and Yuan 2010



Pasquini and Yuan arXiv:1001.5398

Alessandro Bacchetta et al 2010

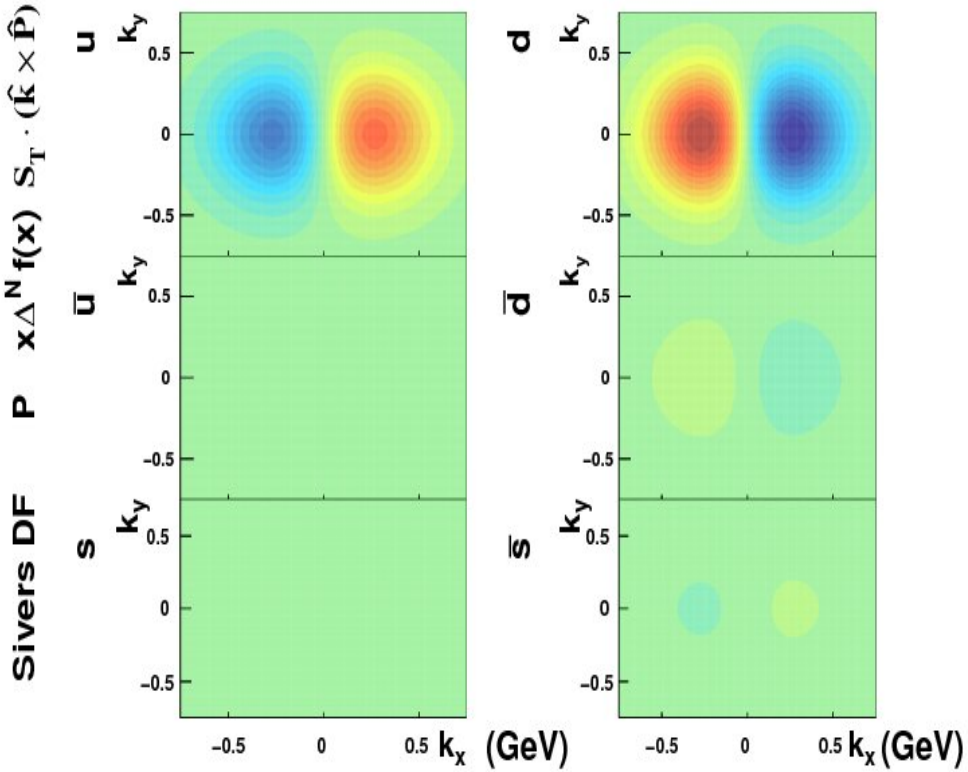


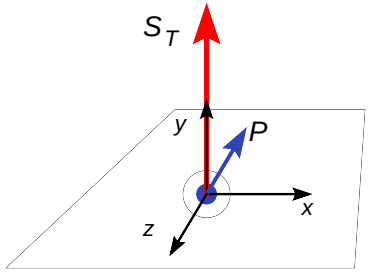
Bacchetta et al arXiv:1003.1328

Reasonable agreement of the extracted Boer-Mulders functions Enzo Barone, Stefano Melis, AP et al 2010 and Lu and Schmidt et al 2009 and model calculations.

Three dimentional picture of the proton

The proton moves along $-Z$ direction (into the screen) and S_T is along Y.





This is the three dimentional view of the proton as "seen" by the virtual photon.
Red color – more quarks. Blue color – less quarks. Distributions of quarks are not symmetrical and shifted due to final state interactions.
$x = 0.2$

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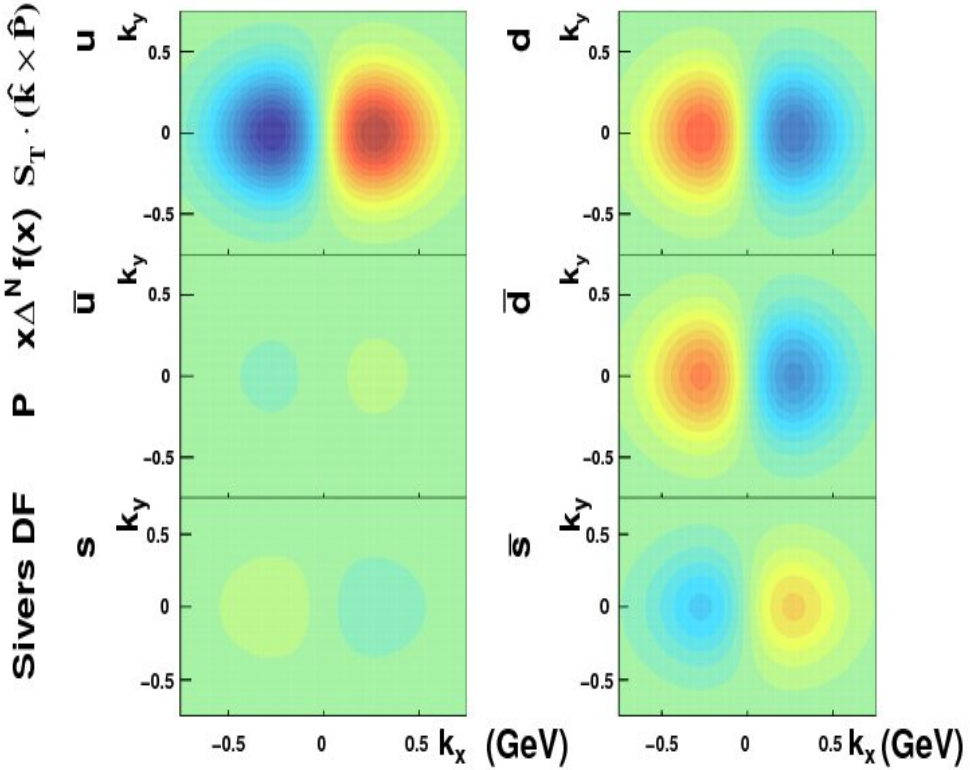

Sivers functions for u, d and sea quarks are extracted from HERMES and COMPASS data. Red color – more quarks. Blue Color – less quarks. Sivers functions is a left – right asymmetry of quark distribution. $x = 0.01$

More information on sea quarks. Future Electron Ion Collider and JLab will contribute.

CONCLUSIONS

- *8* Transverse Momentum Dependent functions describe spin structure of the proton at twist-2.
- Spin Asymmetries are used to study TMDs experimentally.
- T-odd TMDS: Sivers and Boer-Mulders functions have *modified universality*, they change sign from SIDIS to DY.
- HERMES, COMPASS, JLAB, RHIC, and BELLE provide lots of experimental data for TMD extraction.
- Model and lattice QCD calculations of TMDs are possible and match well with TMDs extracted from the experimental data.
- Future facilities sucha s JLab @ 12 GeV, Electron Ion Collider and GSI will contribute to unravel three dimensional structure of the proton.

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